Lecture 9



Introduction to Programming Methods

CS 2: Introduction to Programming Methods

Trees

Outline

- 1 LinkedLists to BinaryTrees
- 2 Why Do We Care About Binary Trees?
- 3 Printing Recursively
- 4 Introducing BSTs
- 5 BST Methods

Consider the following standard LinkedList:



| | Recall the definition of a ListNode |
|---|---|
| 1 | <pre>public class Node {</pre> |
| 2 | public int data; |
| 3 | public Node next; |
| 4 | |
| 5 | <pre>public Node(int data, Node next) {</pre> |
| 5 | this.data = data; |
| 7 | <pre>this.next = next;</pre> |
| 3 | } |
| 9 | } |

Consider the following standard LinkedList:



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| 4 | |
| 5 | <pre>public Node(int data, Node next) {</pre> |
| 6 | this.data = data; |
| 7 | <pre>this.next = next;</pre> |
| 8 | } |
| 9 | } |

What if we added more fields?

- Multiple data fields?
- Multiple "next" fields?

Nodes with Multiple next Fields

```
public class Node {
   public int data;
   public Node next1;
   public Node next2;
   public Node(int data, Node next1, Node next2) {
     this.data = data;
     this.next1 = next1;
     this.next2 = next2;
   }
}
```



Introducing Trees

Binary Trees

```
public class Node {
    public int data;
    public Node left;
    public Node right;
    public Node(int data, Node left, Node right) {
        this.data = data;
        this.left = left;
        this.right = right;
    }
}
```



(red is right; yellow is left)

Back To LinkedLists

Consider the following LinkedList of a mathematical expression:



What's bad about it?

Back To LinkedLists

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- Looking at it doesn't really show us what's going on

Back To LinkedLists

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- Looking at it doesn't really show us what's going on

What about this structure instead?



Now we can see the order of operations much more clearly!

Uses of Trees

■ Parsing (Programming Languages, Math, etc.)

Uses of Trees

Parsing (Programming Languages, Math, etc.)





Uses of Trees

Parsing (Programming Languages, Math, etc.)





Directory File Structure



More Uses of Trees

Recursive Trees (including things like games of Tic-Tac-Toe)



Printing A LinkedList (Again)

```
1 public void print() {
2 Node current = this.front;
3 while (current != null) {
4 System.out.print(current.data + " ");
5 current = current.next;
6 }
7 }
```

We'd like to figure out how to print trees. Since LinkedLists are "simpler versions of trees", they might help.

Printing A LinkedList (Again)

```
1 public void print() {
2 Node current = this.front;
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```

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How do we go in every direction in a tree?

USE RECURSION!

Printing a LinkedList Recursively

To print a LinkedList...

- Print the front of the list
- Print the **next** of the list (recursively)

Code

```
1 public void print() {
2     print(this.front);
3 }
4
5 public void print(Node c) {
6     if (c != null) {
7        System.out.print(c.data + " ");
8     print(c.next);
9     }
10 }
```

Printing a Tree Recursively

To print a BinaryTree...

- Print the root of the tree
- Print the **left** of the tree (recursively)
- Print the right of the tree (recursively)

Code

```
1 public void print() {
2     print(this.root);
3 }
4
5 public void print(Node c) {
6     if (c != null) {
7        System.out.print(c.data + " ");
8     print(c.left);
9     print(c.right);
10     }
11 }
```

Binary Tree methods are just normal recursive functions. The base case/recursive calls will always be similar.

```
Writing a Binary Tree Method
```

```
The base case is current == null.
```

- First recursive case is method(current.left)
- Second recursive case is method(current.right)

```
1
   public type method(...) {
2
      return method(this.root, ...);
3
   }
   private type method(TreeNode current, ...) {
4
5
      if (current == null) { /* D0 BASE CASE */ }
6
7
      // Do the left recursive case:
8
      type leftResult = method(current.left, ...);
9
10
      // Do the right recursive case:
11
      type rightResult = method(current.right, ...);
12
      /* Use the left and right results... */
13
      return ...;
14
<u>15</u>}
```

Binary Tree contains()

contains()

Write a method, in the IntTree class, called contains():

```
public boolean contains(int value);
```

that returns true if the tree contains value and false otherwise.

Binary Tree contains()

16 }

```
contains()
   Write a method, in the IntTree class, called contains():
                 public boolean contains(int value);
   that returns true if the tree contains value and false otherwise.
   public boolean contains(int value) {
 1
2
      return contains(this.root. value):
   }
4
   private boolean contains(Node current, int value) {
5
      /* If the tree is null, it definitely doesn't contain value... */
6
      if (current == null) { return false; }
7
8
      /* If current *is* value, we found it! */
9
      else if (current.data == value) { return true: }
10
11
      else {
```

```
12 boolean leftContainsValue = contains(current.left, value);
13 boolean rightContainsValue = contains(current.right, value);
14 return leftContainsValue || rightContainsValue;
15 }
```

11

Back to contains

12

Recall contains()



Runtime of contains(7)

Consider the following tree:



Back to contains

12

Recall contains()



Runtime of contains(7)



Back to contains

Recall contains()



Runtime of contains(7)



That makes the code $\mathcal{O}(n)$. Can we do better?

In general, we can't do better. BUT, sometimes, we can!

Definition (Binary **SEARCH** Tree (BST))

A binary tree is a \boldsymbol{BST} when an $\boldsymbol{in}\boldsymbol{-order}$ traversal of the tree yields a sorted list.

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To put it another way, a binary tree is a **BST** when:

- All data "to the left of" a node is less than it
- All data "to the right of" a node is greater than it
- All sub-trees of the binary tree are also BSTs

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contains (AGAIN!)

Write contains() for a BST

Fix contains so that it takes advantage of the BST properties.

contains (AGAIN!)

Write contains() for a BST

Fix contains so that it takes advantage of the BST properties.

Recall contains()

```
private boolean contains(IntTreeNode current, int value) {
 2
      /* If the tree is null, it definitely doesn't contain value... */
      if (current == null) { return false; }
4
      /* If current *is* value. we found it! */
6
      else if (current.data == value) { return true: }
7
8
9
      else if (current.data < value) {</pre>
          return contains(current.right, value);
10
      }
11
      else {
12
          return contains(current.left. value);
13
      }
14
```

Runtime of (better) contains(7)

Consider the following tree:



Runtime of (better) contains(7)





WARNING!





WARNING!

Consider the following tree:



This is the same tree, but now we have to visit all the nodes!

Adding to a BST!



Adding to a BST (Attempt #1)

Attempt #1

```
public void add(int value) {
 2
       add(this.root, value);
 3
4
   private void add(IntTreeNode current. int value) {
5
       if (current == null) {
 6
          current = new IntTreeNode(value):
7
8
9
       }
       else if (current.data > value) {
          add(current.left. value):
10
11
       else if (current.data < value) {</pre>
12
          add(current.right. value):
13
14
```

What's wrong with this solution?

Just like with LinkedLists where we must change front or .next, we're not actually changing anything here. We're discarding the result.

Consider the following code:

```
public static void main(String[] args) {
1
2
     String s = "hello world";
3
     s.toUpperCase();
```

```
4
5
      System.out.println(s);
```

Consider the following code:

```
1 public static void main(String[] args) {
2 String s = "hello world";
3 s.toUpperCase();
4 System.out.println(s);
5 }
_______OUTPUT _______
```

>> hello world

Consider the following code:

```
1 public static void main(String[] args) {
2 String s = "hello world";
3 s.toUpperCase();
4 System.out.println(s);
5 }
```

>> hello world

```
1 public static void main(String[] args) {
2 String s = "hello world";
3 s = s.toUpperCase();
4 System.out.println(s);
5 }
```

Consider the following code:



We must USE the result; otherwise, it gets discarded

If you want to write a method that can change the object that a variable refers to, you must do three things:

- 1 Pass in the original state of the object to the method
- 2 Return the new (possibly changed) object from the method
- 3 Re-assign the caller's variable to store the returned result

```
1 p = change(p); // in main
2 public static Point change(Point thePoint) {
3 thePoint = new Point(99, -1);
4 return thePoint;
5 }
```

Adding to a BST (Fixed)

Fixed Attempt

```
public void add(int value) {
 2
       this.root = add(this.root, value);
3
4
   private IntTreeNode add(IntTreeNode current. int value) {
5
       if (current == null) {
6
7
8
9
          current = new IntTreeNode(value):
       }
       else if (current.data > value) {
          current.left = add(current.left, value);
10
       }
11
       else if (current.data < value) {</pre>
12
          current.right = add(current.right, value);
13
14
       return current:
15 }
```

This works because we always update the result, always return the result, and always update the root.